



29. A capacitor  $C$  is first charged fully with potential difference of  $V_0$  and disconnected from the battery. The charged capacitor is connected across an inductor having inductance  $L$ . In  $t$  s 25% of the initial energy in the capacitor is transferred to the inductor. The value of  $t$  is \_\_\_\_\_ s.

(1)  $\frac{\pi\sqrt{LC}}{3}$       (2)  $\frac{\pi\sqrt{LC}}{6}$   
 (3)  $\frac{\pi\sqrt{LC}}{2}$       (4)  $\pi\sqrt{\frac{LC}{2}}$

**Ans. (2)**

**Sol.**  $U_{c_f} = 75\%U_{c_i}$

$$Q_F^2 = \frac{3}{4}Q_I^2$$

$$Q_i \cos \omega t = \frac{\sqrt{3}}{2}Q_i \Rightarrow t = \frac{T}{12}$$

$$t = \frac{\pi}{6}\sqrt{LC}$$

30. The r.m.s speed of oxygen molecules at  $47^\circ\text{C}$  is equal to that of the hydrogen molecules kept at \_\_\_\_\_  $^\circ\text{C}$ . (Mass of oxygen molecule/mass of hydrogen molecule =  $32/2$ )

(1)  $-235$       (2)  $-100$   
 (3)  $-253$       (4)  $-20$

**Ans. (3)**

**Sol.**  $V_{rms} = \sqrt{\frac{3RT}{M}}$



$$V_{rmsO_2} = V_{rmsH_2}$$

$$T_{O_2} = 273 + 47 = 320\text{ K}$$

$$\sqrt{\frac{3RT_{O_2}}{M_{O_2}}} = \sqrt{\frac{3RT_{H_2}}{M_{H_2}}}$$

$$\frac{T_2}{M_{O_2}} = \frac{T_{H_2}}{M_{H_2}}$$

$$\frac{320}{32} = \frac{T_{H_2}}{2}$$

$$T_{H_2} = 20\text{ K}$$

$$T_{H_2} = -253^\circ\text{C}$$

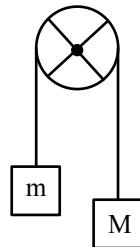
31. Two cars A and B each of mass  $10^3$  kg are moving on parallel tracks separated by a distance of 10 m, in same direction with speeds 72 km/h and 36 km/h. The magnitude of angular momentum of car A with respect to car B is \_\_\_\_\_ J.s.

(1)  $3.6 \times 10^5$       (2)  $10^5$   
 (3)  $3 \times 10^5$       (4)  $2 \times 10^5$

**Ans. (2)**

**Sol.**  $L = m \cdot V_{rel} \cdot r_{\perp}$   
 $= 1000 \times \left( 36 \times \frac{5}{18} \right) \times 10$   
 $= 10^5 \text{ kg m}^2/\text{s}$

32. The pulley shown in figure is made using a thin rim and two rods of length equal to diameter of the rim. The rim and each rod have a mass of  $M$ . Two blocks of mass of  $M$  and  $m$  are attached to two ends of a light string passing over the pulley, which is hinged to rotate freely in vertical plane about its centre. The magnitudes of the acceleration experienced by the blocks is \_\_\_\_\_ (assume no slipping of string on pulley.)



(1)  $\frac{(M-m)g}{\left[\left(\frac{13}{6}\right)M+m\right]}$

(2)  $\frac{(M-m)g}{M+m}$

(3)  $\frac{(M-m)g}{\left[\left(\frac{8}{3}\right)M+m\right]}$

(4)  $\frac{(M-m)g}{2M+m}$

**Ans. (3)**



37. A spherical body of radius  $r$  and density  $\sigma$  falls freely through a viscous liquid having density  $\rho$  and viscosity  $\eta$  and attains a terminal velocity  $v_0$ . Estimated maximum error in the quantity  $\eta$  is : (Ignore errors associated with  $\sigma$ ,  $\rho$  and  $g$ , gravitational acceleration)

(1)  $2\frac{\Delta r}{r} - \frac{\Delta v_0}{v_0}$

(2)  $\frac{2\Delta r}{r} + \frac{\Delta v_0}{v_0}$

(3)  $2\left[\frac{\Delta r}{r} + \frac{\Delta v_0}{v_0}\right]$

(4)  $2\left[\frac{\Delta r}{r} - \frac{\Delta v_0}{v_0}\right]$

**Ans. (2)**

**Sol.**  $v_0 = \frac{2r^2g}{9n}(\rho_B - \rho_L)$

$$n = \frac{2r^2g}{9v_0}(\rho_B - \rho_L)$$

$$\frac{\Delta n}{n} = \frac{2\Delta r}{r} + \frac{\Delta v_0}{v_0}$$

38. Surface tension of two liquids (having same densities),  $T_1$  and  $T_2$ , are measured using capillary rise method utilizing two tubes with inner radii of  $r_1$  and  $r_2$  where  $r_1 > r_2$ . The measured liquid heights in these tubes are  $h_1$  and  $h_2$  respectively. [Ignore the weight of the liquid about the lowest point of miniscus]. The heights  $h_1$  and  $h_2$  and surface tensions  $T_1$  and  $T_2$  satisfy the relation :

(1)  $h_1 < h_2$  and  $T_1 = T_2$

(2)  $h_1 = h_2$  and  $T_1 = T_2$

(3)  $h_1 > h_2$  and  $T_1 = T_2$

(4)  $h_1 > h_2$  and  $T_1 < T_2$

**Ans. (1)**

**Sol.**  $h = \frac{2T}{\rho gr}$

$$h \propto \frac{1}{r}$$

If  $r_1 > r_2 \Rightarrow h_2 > h_1$

39. A river of width 200 m is flowing from west to east with a speed of 18 km/h. A boat, moving with speed of 36 km/h in still water, is made to travel one-round trip (bank to bank of the river). Minimum time taken by the boat for this journey and also the displacement along the river bank are \_\_\_\_\_ and \_\_\_\_\_ respectively.

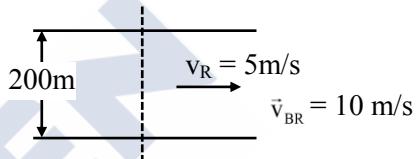
(1) 20 s and 100 m

(2) 40 s and 0 m

(3) 40 s and 200 m

(4) 40 s and 100 m

**Ans. (3)**



**Sol.**

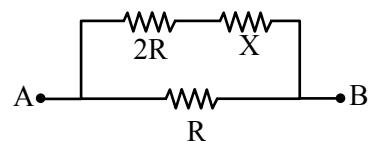
Minimum time :

$$t_{\min} = \frac{200}{10} = 20 \text{ sec}$$

For round trip = 40 sec.

Displacement along river bank =  $40 \times 5 = 200 \text{ m}$

40. Two known resistance of  $R \Omega$  and  $2R \Omega$  and one unknown resistance  $X \Omega$  are connected in a circuit as shown in the figure. If the equivalent resistance between points A and B in the circuit is  $X \Omega$ , then the value of  $X$  is \_\_\_\_\_  $\Omega$ .



(1)  $(\sqrt{3} - 1)R$

(2)  $R$

(3)  $2(\sqrt{3} - 1)R$

(4)  $(\sqrt{3} + 1)R$

**Ans. (1)**

**Sol.**  $\frac{(2R + x).(R)}{3R + x} = x$

$$x^2 + 2Rx - 2R^2 = 0$$

$$x = (\sqrt{3} - 1)R$$

41. The energy of an electron in an orbit of the Bohr's atom is  $-0.04E_0\text{eV}$  where  $E_0$  is the ground state energy. If  $L$  is the angular momentum of the electron in this orbit and  $h$  is the Planck's constant, then  $\frac{2\pi L}{h}$  is \_\_\_\_\_ :

Ans. (3)

**Sol.** Angular momentum  $L = \frac{nh}{2\pi}$

$$n = \frac{2\pi L}{h}$$

$$\text{Energy } E = -\frac{13.6}{n^2} \cdot z^2$$

$$E \Rightarrow -\frac{E_0}{n^2} = -0.04E_0$$

$$n^2 = 25, \quad n = 5$$

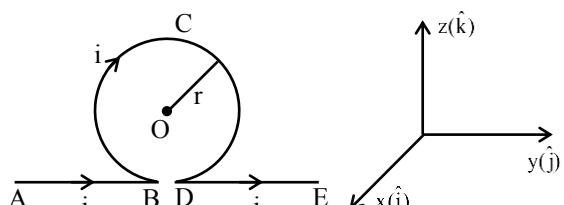
42. An infinitely long straight wire carrying current  $I$  is bent in a planer shape as shown in the diagram. The radius of the circular part is  $r$ . The magnetic field at the centre  $O$  of the circular loop is :

$$(1) \frac{\mu_0}{2\pi} \frac{I}{r} (\pi + 1) \hat{i} \quad (2) -\frac{\mu_0}{2\pi} \frac{I}{r} (\pi - 1) \hat{i}$$

$$(3) \frac{\mu_0}{2\pi} \frac{I}{r} (\pi - 1) \hat{i} \quad (4) -\frac{\mu_0}{2\pi} \frac{I}{r} (\pi + 1) \hat{i}$$

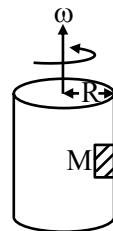
**Ans. (2)**

**Sol.**



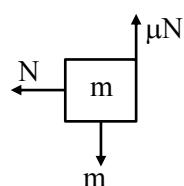
$$\begin{aligned}
 \vec{B}_0 &= \vec{B}_{AB} + \vec{B}_{DE} + \vec{B}_{BCD} \\
 &= \frac{\mu_0 i}{4\pi r} \hat{i} + \frac{\mu_0 i}{4\pi r} \hat{i} - \frac{\mu_0 i}{2r} \hat{i} \\
 &= \frac{\mu_0 i}{2\pi r} \hat{i} - \frac{\mu_0 i}{2r} \hat{i} \\
 &= \frac{\mu_0 i}{2\pi r} (1 - \pi) \hat{i} \\
 &= -\frac{\mu_0 i}{2\pi r} (\pi - 1) \hat{i}
 \end{aligned}$$

43. A large drum having radius  $R$  is spinning around its axis with angular velocity  $\omega$ , as shown in figure. The minimum value of  $\omega$  so that a body of mass  $M$  remains stuck to the inner wall of the drum, taking the coefficient of friction between the drum surface and mass  $M$  is  $\mu$ , is :



(1)  $\sqrt{\frac{\mu g}{R}}$       (2)  $\sqrt{\frac{2g}{\mu R}}$   
 (3)  $\sqrt{\frac{g}{2\mu R}}$       (4)  $\sqrt{\frac{g}{\mu R}}$

Ans. (4)



Sol.

$$N = m\omega^2 r, mg = \mu N$$

$$\mu \times m\omega^2 r = mg$$

$$\omega = \sqrt{\frac{g}{\mu r}}$$

44. A body of mass 2 kg is moving along x-direction such that its displacement as function of time is given by  $x(t) = \alpha t^2 + \beta t + \gamma m$ , where  $\alpha = 1 \text{ m/s}^2$ ,  $\beta = 1 \text{ m/s}$  and  $\gamma = 1 \text{ m}$ . The work done on the body during the time interval  $t = 2 \text{ s}$  to  $t = 3 \text{ s}$ , is \_\_\_\_\_ J.  
 (1) 49 (2) 42  
 (3) 24 (4) 12

**Ans. (3)**

**Sol.**  $x(t) = t^2 + t + 1$

$v(t) = 2t + 1$

$a(t) = 2$

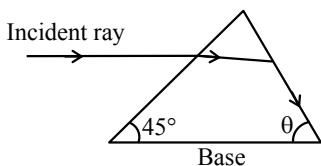
$F = 4 \text{ N}$

$\text{Displacement} = x(3) - x(2)$

$= 13 - 7 = 6 \text{ m}$

$W = F.S = 4 \times 6 = 24 \text{ J}$

45. As shown in the diagram, when the incident ray is parallel to base of the prism, the emergent ray grazes along the second surface.

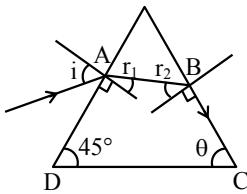


If refractive index of the material of prism is  $\sqrt{2}$ , the angle  $\theta$  of prism is.

(1)  $60^\circ$  (2)  $75^\circ$   
 (3)  $90^\circ$  (4)  $45^\circ$

**Ans. (1)**

**Sol.**



For grazing emergence

$\sin r_2 = \frac{1}{\mu}$

By Snell's Law at incident surface

$1 \times \frac{1}{\sqrt{2}} = \sqrt{2} \sin r_1$

$r_1 = 30^\circ$

$r_1 + r_2 = A$

$A = 75^\circ$

$75 + 45 + \theta = 180^\circ$

$\theta = 60^\circ$

## SECTION-B

46. An electromagnetic wave of frequency 100 MHz propagates through a medium of conductivity,  $\sigma = 10 \text{ mho/m}$ . The ratio of maximum conducting current density to maximum displacement current density is \_\_\_\_\_.

$$\left[ \text{Take } \frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ Nm}^2 / \text{C}^2 \right]$$

**Ans. (1800)**

**Sol.** A

$j_c = \sigma E$

$E \Rightarrow E_0 \sin(\omega t - kx)$

$j_c = \sigma E_0 \sin(\omega t - kx)$

$\Rightarrow (j_c)_{\max} = \sigma E_0 \quad \dots \text{(i)}$

$J_d \Rightarrow \frac{i_d}{A} = \frac{1}{A} \times \epsilon_0 \frac{AdE}{dt}$

$\Rightarrow \epsilon_0 \times E_0 \omega \cos(\omega t - kx)$

$(j_d)_{\max} \Rightarrow \epsilon_0 E_0 \omega \quad \dots \text{(ii)}$

(i)/(ii)

$$\frac{(j_c)_{\max}}{(j_d)_{\max}} = \frac{\sigma E_0}{\epsilon_0 \omega E_0} \Rightarrow \frac{\sigma}{\epsilon_0 \omega}$$

$\Rightarrow \frac{10 \times 4\pi \times 9 \times 10^9}{2\pi \times 100 \times 10^6}$

$\Rightarrow 1800$

47. The terminal velocity of a metallic ball of radius 6 mm in a viscous fluid is 20 cm/s. The terminal velocity of another ball of same material and having radius 3 mm in the same fluid will be \_\_\_\_\_ cm/s.

**Ans. (5)**

**Sol.** We know :

$\text{Terminal velocity} \propto (\text{radius})^2$

$$\frac{(v_T)_1}{(v_T)_2} = \left( \frac{6}{3} \right)^2$$

$$(v_T)_2 = \frac{(v_T)_1}{4} = 5 \text{ cm/sec}$$

48. A particle having electric charge  $3 \times 10^{-19}$  C and mass  $6 \times 10^{-27}$  kg is accelerated by applying an electric potential of 1.21 V. Wavelength of the matter wave associated with the particle is  $\alpha \times 10^{-12}$  m. The value of  $\alpha$  is \_\_\_\_\_.  
 (Take Planck's constant =  $6.6 \times 10^{-34}$  J.s)

**Ans. (10)**

**Sol.**  $\lambda = \frac{h}{\sqrt{2mqV}}$

$$\lambda = \frac{6.6 \times 10^{-34}}{\sqrt{2 \times 18 \times 10^{-46} \times 1.21}}$$

$$\lambda = 10^{-11} \text{ m} = 10 \times 10^{-12} \text{ m}$$

$$\alpha = 10$$

49. In a Young's double slit experiment set up, the two slits are kept 0.4 mm apart and screen is placed at 1 m from slits. If a thin transparent sheet of thickness  $20 \mu\text{m}$  is introduced in front of one of the slits then centre bring fringe shifts by 20 mm on the screen. The refractive index of transparent sheet is given by  $\frac{\alpha}{10}$ , where  $\alpha$  is \_\_\_\_\_.  
 (Take  $\lambda = 600 \text{ nm}$ )

**Ans. (14)**

**Sol.**  $y_{\text{shift}} = \frac{(\mu-1)tD}{d}$

$$20 \times 10^{-3} = \frac{(\mu-1) \times 20 \times 10^{-6} \times 1}{0.4 \times 10^{-3}}$$

$$(\mu-1) \Rightarrow 0.4$$

$$\mu \Rightarrow 1.4$$

$$\frac{\alpha}{10} = 1.4, \alpha = 14$$

50. A diatomic gas ( $\gamma = 1.4$ ) does 100 J of work when it is expanded isobarically. Then the heat given to the gas \_\_\_\_\_ J.

**Ans. (350)**

**Sol.**  $w = 100 \text{ J} = nR\Delta T$  for isobaric process.

$$Q = nC_p \Delta T = \left( \frac{f}{2} + 1 \right) nR\Delta T$$

$$= \frac{7}{2} \cdot (100) = 350 \text{ Joule.}$$

