

(1) $\frac{200}{\sqrt{3}}$ (2) $200\sqrt{6}$
 (3) $200\sqrt{3}$ (4) $100\sqrt{3}$

Ans. (3)

Sol. From continuity equation

$$A_A V_A = A_B V_B \Rightarrow 6V_A = 3V_B \Rightarrow V_B = 2V_A$$

Applying Bernoulli's equation between A & B,

$$P_A + \frac{1}{2}\rho V_A^2 = P_B + \frac{1}{2}\rho V_B^2$$

$$\Rightarrow \rho g \times 0.05 = \frac{1}{2}\rho [V_B^2 - V_A^2] = \frac{1}{2}\rho (3V_A^2)$$

$$\Rightarrow V_A = \sqrt{\frac{2g \times 0.05}{3}} \text{ m/s} = \frac{1}{\sqrt{3}} \text{ m/s} = \frac{100}{\sqrt{3}} \text{ cm/s}$$

$$\Rightarrow \text{Volume flow rate} = A_A V_A = \frac{6 \times 100}{\sqrt{3}} \text{ cm}^3/\text{sec}$$

$$= 200\sqrt{3} \text{ cm}^3/\text{sec}$$

Correct option (3)

30. In an experiment the values of two spring constants were measured as $k_1 = (10 \pm 0.2) \text{ N/m}$ and $k_2 = (20 \pm 0.3) \text{ N/m}$. If these springs are connected in parallel, then the percentage error in equivalent spring constant is :
 (1) 2.67% (2) 2.33%
 (3) 1.33% (4) 1.67%

Ans. (4)

Sol. For parallel combination of spring,

$$K_{\text{eq}} = K_1 + K_2 = 30 \text{ N/m}$$

$$\Delta K_{\text{eq}} = \Delta K_1 + \Delta K_2 = 0.2 + 0.3 = 0.5 \text{ N/m}$$

$$\therefore \% \text{Error in } K = \frac{0.5}{30} \times 100 = 1.67\%$$

Correct option (4)

31. A 4 kg mass moves under the influence of a force $\vec{F} = (4t^3\hat{i} - 3t\hat{j}) \text{ N}$ where t is the time in second. If mass starts from origin at $t = 0$, the velocity and position after $t = 2\text{s}$ will be :

$$(1) \vec{v} = 3\hat{i} + \frac{3}{2}\hat{j} \quad \vec{r} = \frac{6}{5}\hat{i} + \hat{j}$$

$$(2) \vec{v} = 4\hat{i} - \frac{3}{2}\hat{j} \quad \vec{r} = \frac{8}{5}\hat{i} - \hat{j}$$

$$(3) \vec{v} = 4\hat{i} + \frac{5}{2}\hat{j} \quad \vec{r} = \frac{8}{5}\hat{i} + 2\hat{j}$$

$$(4) \vec{v} = 4\hat{i} - \frac{3}{2}\hat{j} \quad \vec{r} = \frac{6}{5}\hat{i} - \hat{j}$$

Ans. (2)

Sol. $\vec{F} = 4t^3\hat{i} - 3t\hat{j}$

$$\vec{a} = \frac{\vec{F}}{m} = t^3\hat{i} - \frac{3}{4}\hat{j}$$

$$a_x = t^3$$

$$\frac{dv_x}{dt} = t^3$$

$$\int_{v_{x_2}}^{v_{x_2}} dv_x = \int_{t=0}^{t=2} t^3 dt$$

$$v_{x_2} - 0 = \left[\frac{t^4}{4} \right]_0^2$$

$$v_{x_2} = 4$$

$$a_y = \frac{-3}{4}t$$

$$\frac{dv_y}{dt} = -\frac{3}{4}t$$

$$\int_0^{v_{y_2}} dv_y = \int_0^2 -\frac{3}{4}t dt$$

$$v_{y_2} = -\frac{3}{4} \left[\frac{t^2}{2} \right]_0^2$$

$$v_{y_2} = -\frac{3}{2}$$

$$\vec{v}_2 = 4\hat{i} - \frac{3}{2}\hat{j}$$

$$v_x = \frac{t^4}{4}$$

$$\int_0^{x_2} dx = \int_0^2 \frac{t^4}{4} dt$$

$$x_2 - 0 = \left[\frac{t^5}{20} \right]_0^2$$

$$x_2 = \frac{8}{5}$$

$$v_y = \frac{-3}{8}t^2$$

$$\int_0^{y_2} dx = \frac{-3}{8}t^2 dt$$

$$y_2 - 0 = \frac{-3}{8} \left[\frac{t^3}{3} \right]_0^2$$

$$y_2 = -1$$

$$\vec{r} = \frac{8}{5}\hat{i} - \hat{j}$$

Correct option (2)

35. The electric field of a plane electromagnetic wave is given by :

$$E_y = 69 \sin[0.6 \times 10^3 x - 1.8 \times 10^{11} t] \text{ V/m.}$$

The expression for magnetic field associated with this electromagnetic wave is _____ T.

- (1) $B_z = 2.3 \times 10^{-7} \sin[0.6 \times 10^3 x - 1.8 \times 10^{11} t]$
- (2) $B_z = 2.3 \times 10^{-7} \sin[0.6 \times 10^3 x + 1.8 \times 10^{11} t]$
- (3) $B_y = 69 \sin[0.6 \times 10^3 x + 1.8 \times 10^{11} t]$
- (4) $B_y = 2.3 \times 10^{-7} \sin[0.6 \times 10^3 x - 1.8 \times 10^{11} t]$

Ans. (1)

Sol. $\hat{B} = \hat{c} \times \hat{E}$

$\Rightarrow \hat{c} = \hat{i}$ because phase of electric field is function of x.

$\Rightarrow \hat{E} = \hat{j}$ (given)

$\Rightarrow \hat{B} = \hat{i} \times \hat{j} = \hat{k}$

$$|B| = \frac{|E|}{c} = \frac{69 \times 0.6 \times 10^3}{1.8 \times 10^{11}} = \frac{69}{3 \times 10^8}$$

$$|B| = 2.9 \times 10^{-7}$$

$$\vec{B}_2 = 2.9 \times 10^{-7} \sin(0.6 \times 10^3 x - 1.8 \times 10^{11} t)$$

(phase is same as that of electric field)

Correct option (1)

36. In a double slit experiment the distance between the slits is 0.1 cm and the screen is placed at 50 cm from the slits plane. When one slit is covered with a transparent sheet having thickness t and refractive index $n(= 1.5)$, the central fringe shifts by 0.2 cm. The value of t is _____ cm.

- (1) 8×10^{-4}
- (2) 6.0×10^{-3}
- (3) 5.6×10^{-4}
- (4) 5.0×10^{-3}

Ans. (1)

Sol. $ds \sin \theta = (\mu - 1)t$

$$d \left[\frac{x}{D} \right] = (\mu - 1)t$$

$$t = \frac{xd}{D(\mu - 1)}$$

$$= \frac{(0.2)(0.1)}{50(1.5 - 1)}$$

$$t = 8 \times 10^{-4} \text{ cm}$$

Correct option (1)

37. A light wave described by $E = 60 \sin(3 \times 10^{15} t + \sin(12 \times 10^{15} t))$ (in SI units) falls on a metal surface of work function 2.8 eV. The maximum kinetic energy of ejected photoelectron is (approximately) _____ eV. ($h = 6.6 \times 10^{-34} \text{ J-s}$ and $e = 1.6 \times 10^{-19} \text{ C}$)

- (1) 5.1
- (2) 3.8
- (3) 6.0
- (4) 7.8

Ans. (1)

Sol. $\omega_i = 3 \times 10^{15} \text{ rad/sec}$

$$\omega_2 = 12 \times 10^{15} \text{ rad/sec}$$

$$\therefore v = \frac{\omega}{2\pi}$$

$$E_{\text{photon}} = hv = 6.6 \times 10^{-34} \times 1.91 \times 10^{15} = 1.26 \times 10^{-18} \text{ J}$$

$$E_{\text{max}} = \frac{1.26 \times 10^{-18}}{1.6 \times 10^{-19}} \approx 7.9 \text{ eV}$$

$$K_{\text{max}} = E_{\text{max}} - \phi_0 = 7.9 - 2.8$$

$$K_{\text{max}} = 5.1 \text{ eV}$$

Correct option (1)

38. If an alpha particle with energy 7.7 MeV is bombarded on a thin gold foil, the closest distance from nucleus it can reach is _____ m.

$$(\text{Atomic number of gold} = 79 \text{ and } \frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ in SI units})$$

- (1) 2.95×10^{-14}
- (2) 2.95×10^{-16}
- (3) 3.85×10^{-16}
- (4) 3.85×10^{-14}

Ans. (1)

Sol. Energy conservation

$$K_i + U_i = K_f + U_f$$

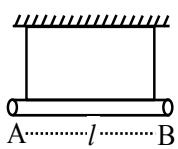
$$7.7 \times 10^6 \times 1.6 \times 10^{-19} + 0$$

$$= 0 + \frac{9 \times 10^9 (1.6 \times 10^{-19}) (79 \times 1.6 \times 10^{-19})}{r}$$

$$r = 2.95 \times 10^{-14}$$

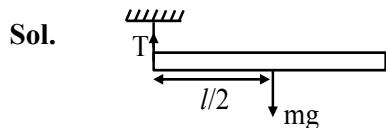
Correct option (1).

39. A uniform rod of mass m and length l suspended by means of two identical inextensible light strings as shown in figure. Tension in one string immediately after the other string is cut, is _____. (g acceleration due to gravity)



(1) $mg/2$ (2) $mg/4$
 (3) $mg/3$ (4) mg

Ans. (2)



$$mg \frac{l}{2} = \frac{ml^2}{3} \alpha$$

$$\alpha = \frac{3g}{2l} \quad \dots(1)$$

$$mg - T = ma_c$$

$$T = mg - ma_c$$

$$= mg - m \left(\frac{l}{2} \alpha \right)$$

$$= mg - m \left(\frac{l}{2} \cdot \frac{3g}{2l} \right)$$

$$T = \frac{mg}{4}$$



Correct option (2)

40. An aluminium and steel rods having same lengths and cross-sections are joined to make total length of 120 cm at 30°C. The coefficient of linear expansion of aluminium and steel are $24 \times 10^{-6}/^\circ\text{C}$ and $1.2 \times 10^{-5}/^\circ\text{C}$, respectively. The length of this composite rod when its temperature is raised to 100°C, is ____ cm.

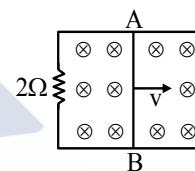
(1) 120.20 (2) 120.15
 (3) 120.03 (4) 120.06

Ans. (2)

Sol. $\ell_{\text{final}} = \ell_0(1 + \alpha_A \Delta T) + \ell_0(1 + \alpha_B \Delta T)$
 $= \ell_0 [2 + (\alpha_A + \alpha_B) \Delta T]$
 $= 60 [2 + (36 \times 10^{-6}) \times 70]$
 $= 60 [2 + 0.0025]$
 $= 120.15 \text{ cm}$

Correct option (2)

41. A 1 m long metal rod AB completes the circuit as shown in figure. The area of circuit is perpendicular to the magnetic field of 0.10 T. If the resistance of the total circuit is 2Ω then the force needed to move the rod towards right with constant speed (v) of 1.5 m/s is ____ N.



(1) 7.5×10^{-2} (2) 5.7×10^{-3}
 (3) 5.7×10^{-2} (4) 7.5×10^{-3}

Ans. (4)

Sol. To maintain constant speed

$$F_{\text{ext}} = F_B$$

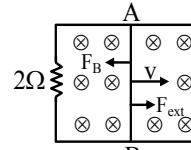
$$\Rightarrow F_{\text{ext}} = iLB$$

$$= \left(\frac{vBl}{R} \right) lB$$

$$= \frac{B^2 l^2 v}{R}$$

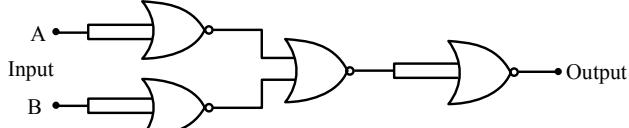
$$= \frac{(0.1)^2 \times (1)^2 \times 1.5}{2}$$

$$= 7.5 \times 10^{-3} \text{ N}$$



Correct option (4)

42. The given circuit works as :



(1) AND gate (2) NOR gate
 (3) NAND gate (4) OR gate

Ans. (3)

Now, $r_f = \sqrt{(2-0)^2 + (2-0)^2 + (1-0)^2} = 3 \text{ m}$

$$r_i = \sqrt{(4-0)^2 + (4-0)^2 + (2-0)^2} = 6 \text{ m}$$

$$\therefore W_{\text{ext}} = (9 \times 10^9) \times (10^{-8} \times 2 \times 10^{-6}) \left[\frac{1}{3} - \frac{1}{6} \right]$$

$$= 3 \times 10^{-5}$$

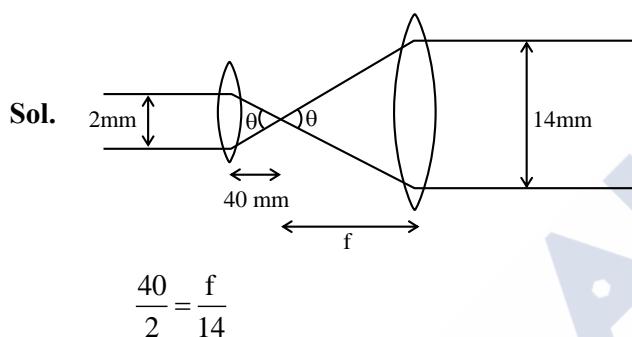
$$= 30 \times 10^{-6} \text{ J}$$

Correct Option (3)

SECTION - B

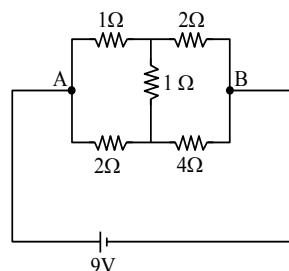
46. A collimated beam of light of diameter 2 mm is propagating along x-axis. The beam is required to be expanded in a collimated beam of diameter 14 mm using a system of two convex lenses. If first lens has focal length 40 mm, then the focal length of second lens is _____ mm.

Ans. (280)



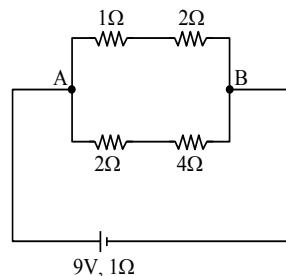
Correct Answer : 280

47. The heat generated in 1 minute between points A and B in the given circuit, when a battery of 9V with internal resistance of 1 Ω is connected across these points is _____ J.

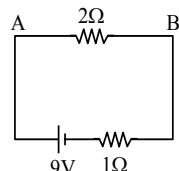


Ans. (1080)

Sol.



Balanced Wheatstone bridge



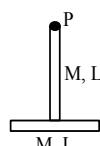
$$i = \frac{9}{3} = 3 \text{ A}$$

$$\therefore H_{AB} = i^2 R_{AB} t$$

$$= (3)^2 \times 2 \times 60 = 1080 \text{ J}$$

Correct Answer : 1080

48. Two identical thin rods of mass $M \text{ kg}$ and length $L \text{ m}$ are connected as shown in figure. Moment of inertia of the combined rod system about an axis passing through point P and perpendicular to the plane of the rods is $\frac{x}{2} ML^2 \text{ kg m}^2$. The value of x is _____.



Ans. (17)

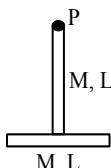
Sol.

$$I = \frac{ML^2}{3} + \left(\frac{ML^2}{12} + ML^2 \right)$$

$$= \frac{4ML^2 + ML^2 + 12ML^2}{12}$$

$$I = \frac{17}{12} ML^2$$

$$\therefore x = 17$$



Correct Answer : 17

49. 10 mole of oxygen is heated at constant volume from 30°C to 40°C . The change in the internal energy of the gas is _____ cal. (The molecular specific heat of oxygen at constant pressure, $C_p = 7 \text{ cal./mol } ^{\circ}\text{C}$ and $R = 2 \text{ cal./mol } ^{\circ}\text{C}$.)

Ans. (500)

Sol. $\Delta U = nC_v \Delta T$

$$= n(C_p - R)\Delta T$$

$$= 10(7 - 2)(40 - 30)$$

$$\Delta U = 500$$

Correct Answer : 500

50. In a microscope the objective is having focal length $f_o = 2 \text{ cm}$ and eye-piece is having focal length $f_e = 4 \text{ cm}$. The tube length is 32 cm. The magnification produced by this microscope for normal adjustment is _____.

Ans. (100)

Sol. $m \approx \frac{f_o f_e}{f_o + f_e}$

$$= \frac{32}{2} \times \frac{25}{4}$$

$$m = 100$$

Correct Answer : 100