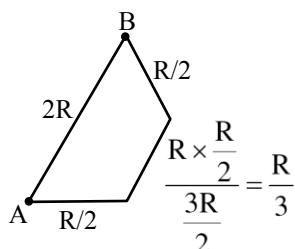
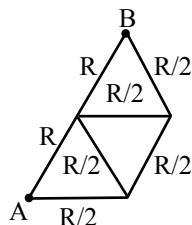
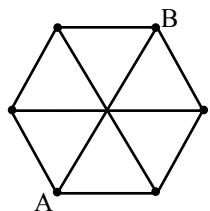
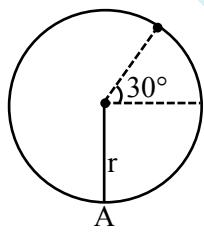


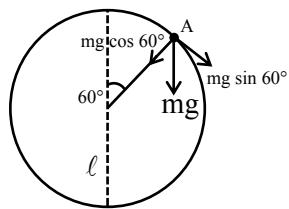
Sol.


$$R_{eq} = \frac{2R \times \frac{4R}{3}}{2R + \frac{4R}{3}} = \frac{8R^2}{10R} = \frac{4}{5}R$$

30. In case of vertical circular motion of a particle by a thread of length r if the tension in the thread is zero at an angle 30° shown in figure, the velocity at the bottom point (A) of the circular path is (g = gravitational acceleration)



(1) $\sqrt{5gr}$ (2) $\sqrt{\frac{7}{2}gr}$
 (3) $\sqrt{4gr}$ (4) $\sqrt{\frac{5}{2}gr}$

Ans. (2)
Sol.


$$T + mg \cos 60^\circ = \frac{mV^2}{l}$$

$$T = 0$$

$$V^2 = \frac{gl}{2} \text{ here } V \text{ is the speed at point A}$$

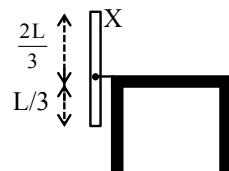
M.E.C.

$$\frac{1}{2}mu^2 = mg(l + l \cos 60^\circ) + \frac{1}{2}mV^2$$

$$u^2 = 3gl + \frac{gl}{2}$$

$$u = \sqrt{\frac{7gl}{2}}$$

31. A thin uniform rod (X) of mass M and length L is pivoted at a height $\left(\frac{L}{3}\right)$ as shown in the figure. The rod is allowed to fall from a vertical position and lie horizontally on the table. The angular velocity of this rod when it hits the table top, is _____. (g = gravitational acceleration)



(1) $\sqrt{\frac{3}{2} \frac{g}{L}}$ (2) $\frac{3}{\sqrt{2}} \sqrt{\frac{g}{L}}$
 (3) $\frac{1}{\sqrt{2}} \sqrt{\frac{g}{L}}$ (4) $\sqrt{\frac{3g}{L}}$

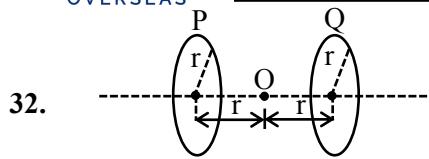
Ans. (4)

$$\text{Sol. } mg \frac{\ell}{6} = \frac{1}{2} I \omega^2$$

$$\text{Here } I = \frac{m\ell^2}{12} + \frac{m\ell^2}{36} = \frac{m\ell^2}{9}$$

$$mg \frac{\ell}{6} = \frac{m\ell^2}{18} \omega^2 \Rightarrow \omega^2 = \frac{3g}{\ell}$$

$$\omega = \sqrt{\frac{3g}{\ell}}$$



32. Two identical circular loops P and Q each of radius r are lying in parallel planes such that they have common axis. The current through P and Q are I and $4I$ respectively in clockwise direction as seen from O. The net magnetic field at O is:

(1) $\frac{3\mu_0 I}{4\sqrt{2}r}$ toward P

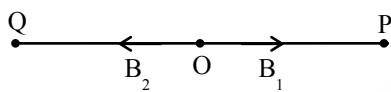
(2) $\frac{\mu_0 I}{4\sqrt{2}r}$ toward P

(3) $\frac{\mu_0 I}{4\sqrt{2}r}$ towards Q

(4) $\frac{3\mu_0 I}{4\sqrt{2}r}$ towards Q

Ans. (4)

Sol. $B_{\text{net}} = B_1 - B_2$



$$= \frac{4\mu_0 i R^2}{2(R^2 + R^2)^{3/2}} - \frac{\mu_0 i R^2}{2(R^2 + R^2)^{3/2}}$$

$$= \frac{3\mu_0 i}{4\sqrt{2}R}$$

33. When a light of a given wavelength falls on a metallic surface the stopping potential for photoelectrons is 3.2 V. If a second light having wavelength twice of first light is used, the stopping potential drops to 0.7 V. The wavelength of first light is _____ m.

$(h = 6.63 \times 10^{-34} \text{ J.s}, e = 1.6 \times 10^{-19} \text{ C}, c = 3 \times 10^8 \text{ m/s})$

(1) 2.9×10^{-8}

(2) 2.2×10^{-8}

(3) 3.1×10^{-7}

(4) 2.5×10^{-7}

Ans. (4)

Sol. $q.(3.2) = \frac{hc}{\lambda} - \phi \quad \dots(1)$

$q(0.7) = \frac{hc}{2\lambda} - \phi \quad \dots(2)$

Eq. (1) – Eq. (2)

$q.(2.5) = \frac{hc}{2\lambda}$

$2.5 = \left(\frac{hc}{e}\right) \left(\frac{1}{2\lambda}\right)$

$2.5 = \frac{12400}{2(\lambda)}$

$\lambda = \frac{12400}{5} \text{ Å}$

$\lambda = 2480 \text{ Å}$

$\lambda = 2.48 \times 10^{-7} \text{ m}$

34. The fifth harmonic of a closed organ pipe is found to be in unison with the first harmonic of an open pipe. The ratio of lengths of closed pipe to that of the open pipe is $5/x$. The value of x is _____.

(1) 4 (2) 2 (3) 1 (4) 3

Ans. (2)

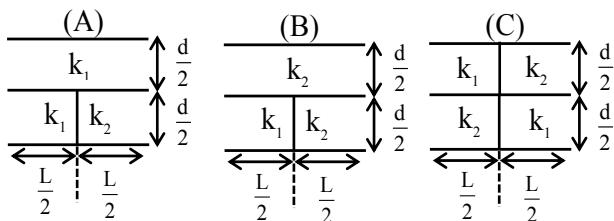
Sol. $f_{5 \text{ closed}} = f_1 \text{ open}$

$$\frac{5v}{4L_{\text{closed}}} = \frac{v}{2L_{\text{open}}}$$

$$\frac{L_{\text{closed}}}{L_{\text{open}}} = \frac{5}{2}$$

$x = 2$

35. Three parallel plate capacitors each with area A and separation d are filled with two dielectric (k_1 and k_2) in the following fashion. Which of the following is true? ($k_1 > k_2$)



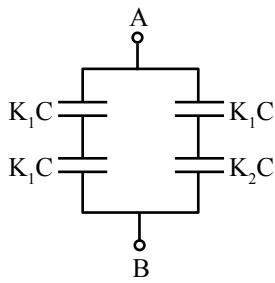
(1) $C_B > C_C > C_A$

(3) $C_C > C_A > C_B$

(2) $C_C > C_B > C_A$

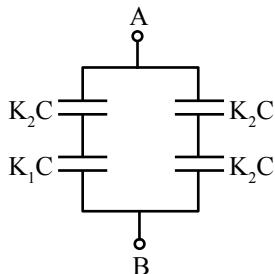
(4) $C_A > C_C > C_B$

Ans. (4)

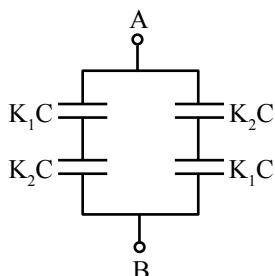


$$\text{Let } \frac{\epsilon_0 A}{d} = C$$

$$\begin{aligned} \therefore C_A &= \frac{K_1 C}{2} + \frac{K_1 K_2 C}{K_1 + K_2} \\ &= K_1 C \left[\frac{K_1 + 2K_2}{2(K_1 + K_2)} \right] \end{aligned}$$

 For C_B :


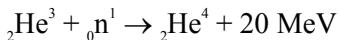
$$\begin{aligned} C_B &= \frac{K_2 C}{2} + \frac{K_1 K_2 C}{K_1 + K_2} \\ &= K_2 C \left[\frac{K_1 + 2K_2}{2(K_1 + K_2)} \right] \end{aligned}$$

 For C_C :


$$C_C = \frac{2K_1 K_2 C}{(K_1 + K_2)}$$

$$C_A > C_C > C_B$$

36. The binding energy for the following nuclear reactions are expressed in MeV.



If X_3 , X_4 , X_5 denote the stability of ${}_2^3\text{He}$, ${}_2^4\text{He}$ and ${}_2^5\text{He}$, respectively, then the correct order is :

- (1) $X_4 > X_5 > X_3$
- (2) $X_4 = X_5 = X_3$
- (3) $X_4 > X_5 < X_3$
- (4) $X_4 < X_5 < X_3$

Ans. (1)

$$\text{Sol. } \text{BE}_{\text{He}^4} - \text{BE}_{\text{He}^3} = 20 \text{ MeV} \quad \dots(1)$$

$$\text{BE}_{\text{He}^5} - \text{BE}_{\text{He}^4} = -0.9 \text{ MeV} \quad \dots(2)$$

From eq (1) & (2)

$$\text{BE}_{\text{He}^4} > \text{BE}_{\text{He}^5} > \text{BE}_{\text{He}^3}$$

$$X_4 > X_5 > X_3$$

37. A cubical block of density $\rho_b = 600 \text{ kg/m}^3$ floats in a liquid of density $\rho_e = 900 \text{ kg/m}^3$. If the height of block is $H = 8.0 \text{ cm}$ then height of the submerged part is _____ cm.

- (1) 7.3
- (2) 4.3
- (3) 6.3
- (4) 5.3

Ans. (4)

$$\text{Sol. } \text{Mg} = F_b$$

$$dAHg = \rho Ahg$$

$$600 \times 8 \text{ cm} = 900 \times h$$

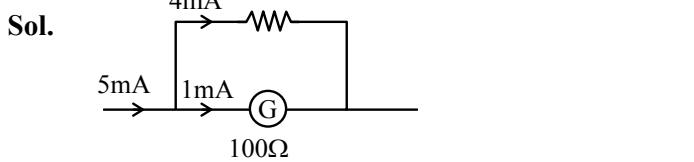
$$h = \frac{16}{3} \text{ cm}$$

$$h = 5.3 \text{ cm}$$

38. A moving coil galvanometer of resistance 100Ω shows a full scale deflection for a current of 1 mA. The value of resistance required to convert this galvanometer into an ammeter, showing full scale deflection for a current of 5 mA, is _____ Ω

- (1) 25
- (2) 10
- (3) 0.5
- (4) 2.5

Ans. (1)



$$G = 100 \Omega$$

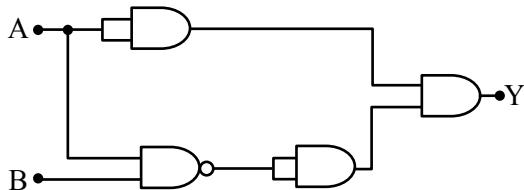
$$i_g = 1 \text{ mA}$$

$$i = 5 \text{ mA}$$

$$r_s = \frac{G}{\left(\frac{i}{i_g} - 1\right)}$$

$$= \frac{100}{\left(\frac{5}{1} - 1\right)} = 25 \Omega$$

39. Identify the correct truth table of the given logical circuit.



(1)

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

(2)

A	B	Y
0	0	1
0	1	0
1	0	1
1	1	0

(3)

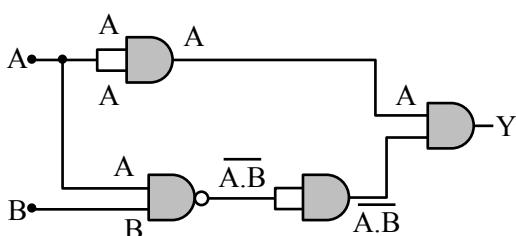
A	B	Y
0	0	1
0	1	1
1	0	1
1	1	0

(4)

A	B	Y
0	0	0
0	1	0
1	0	1
1	1	0

Ans. (4)

Sol.



$$y = A \cdot \overline{A \cdot B}$$

$$= A \cdot (\overline{A} + \overline{B}) = 0 + A\overline{B}$$

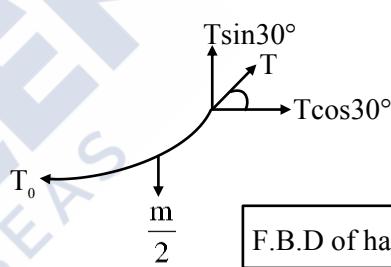
A	B	Y
0	0	0
0	1	0
1	0	1
1	1	0

40. A flexible chain of mass m hangs between two fixed points at the same level. The inclination of the chain with the horizontal at the two points of support is 30° . Considering the equilibrium of each half of the chain, the tension of the chain at the lowest point is ____.

$$(1) \frac{\sqrt{3}}{2}mg \quad (2) \frac{1}{2}mg \quad (3) mg \quad (4) \sqrt{3}mg$$

Ans. (1)

Sol.



F.B.D of half rope

$$T \sin 30^\circ = \frac{m}{2}g$$

$$T \cos 30^\circ = T_0$$

$$\tan 30^\circ = \frac{mg}{2T_0}$$

$$T_0 = \frac{\sqrt{3}}{2}mg$$

41. A point source is kept at the center of a spherically enclosed detector. If the volume of the detector increased by 8 times, the intensity will

(1) increase by 8 times (2) increase by 64 times
(3) decrease by 8 times (4) decrease by 4 times

Ans. (4)

Sol. $V \rightarrow 8V \Rightarrow R \rightarrow 2R$

$$\Rightarrow A \rightarrow 4A$$

$$\Rightarrow I \rightarrow \frac{I_0}{4}$$

42. In the Young's double slit experiment the intensity produced by each one of the individual slits is I_0 . The distance between two slits is 2 mm. The distance of screen from slits is 10 m. The wavelength of light is 6000 Å. The intensity of light on the screen in front of one of the slits is _____.
 (1) $2I_0$ (2) I_0 (3) $\frac{I_0}{2}$ (4) $4I_0$

Ans. (2)

Sol. $d = 2\text{ mm}$

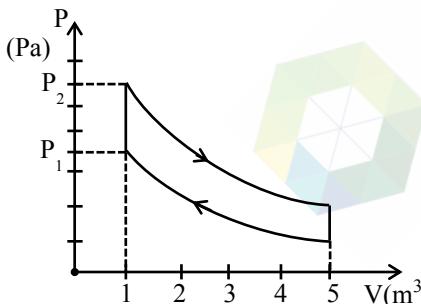
$$D = 10 \text{ m}$$

$$\lambda = 6000 \text{ \AA}$$

$$y = \frac{d}{2} \text{ (in front of one slit)}$$

$$I = 4I_0 \cos^2 \left(\frac{2\pi}{\lambda} \cdot \frac{y}{D} d \right)$$

$$\Rightarrow I = I_0$$

43. 10 mole of an ideal gas is undergoing the process shown in the figure. The heat involved in the process from P_1 to P_2 is α Joule ($P_1 = 21.7 \text{ Pa}$ and $P_2 = 30 \text{ Pa}$, $C_v = 21 \text{ J/K.mol}$, $R = 8.3 \text{ J/mol.K}$). The value of α is _____.


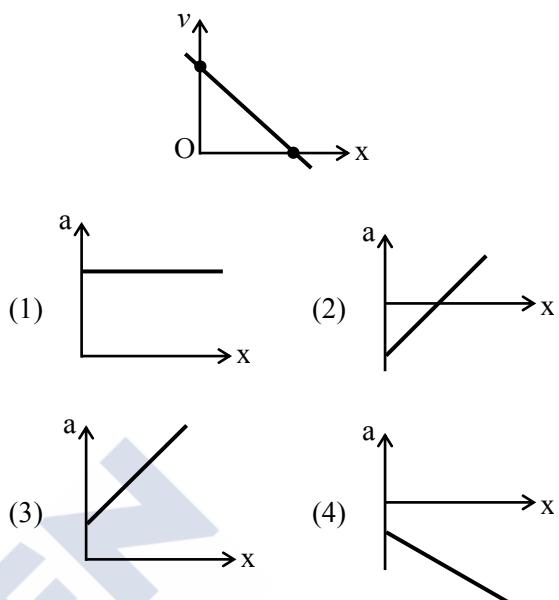
(1) 24 (2) 15 (3) 21 (4) 28

Ans. (3)

Sol. $\Delta Q = nC_v\Delta T$ (isochoric)

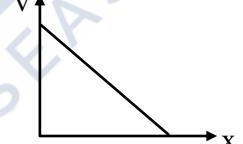
$$\begin{aligned} &= \frac{C_v}{R} \cdot nR\Delta T = \frac{C_v}{R} (P_2 - P_1) V \\ &= \frac{21}{8.3} \times (30 - 21.7) \times 1 = 21 \text{ J} \end{aligned}$$

44. The velocity (v) – Distance (x) graph is shown in figure. Which graph represents acceleration (a) versus distance (x) variation of this system?



Ans. (2)

Sol.



Eq. of V vs x from graph

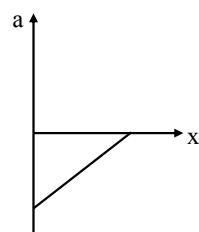
$$V = C_1 - C_2x$$

$$a = V \frac{dV}{dx}$$

$$= (C_1 - C_2x) \times -C_2$$

$$a = C_2^2x - C_1C_2$$

\therefore graph is straight line +ve solve –ve intercept



45. Distance between an object and three times magnified real image is 40 cm. The focal length of the mirror used is ____ cm.
 (1) $-15/2$ (2) -10
 (3) -20 (4) -15

Ans. (4)

Sol. $m = -3 = \frac{v}{u}$

$$v = -3u$$

$$|v| - |u| = 40$$

$$u = 20 \text{ cm}$$

$$v = 60 \text{ cm}$$

$$\therefore \frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{-60} + \frac{1}{-20} = \frac{1}{f}$$

$$f = -15 \text{ cm}$$

SECTION-B

46. When 300 J of heat given to an ideal gas with $C_p = \frac{7}{2}R$ its temperature raises from 20°C to 50°C keeping its volume constant. The mass of the gas is (approximately) ____ g. ($R = 8.314 \text{ J/mol.K}$).

NTA Ans. (481)

Allen Ans. (Bonus)

Sol. $C_v = C_p - R = \frac{5}{2}R$

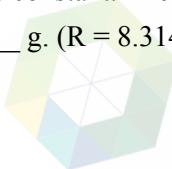
$$\Delta Q = nC_v \Delta T$$

$$300 = n \times \frac{5}{2} \times 8.314 \times 30$$

$$n = 0.48$$

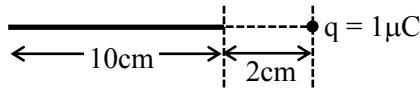
$$\frac{m}{M} = 0.48$$

We cannot find mass (m) because molar mass (M) not given.



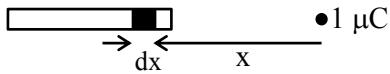
47. A point charge $q = 1 \mu\text{C}$ is located at a distance 2 cm from one end of a thin insulating wire of length 10 cm having a charge $Q = 24 \mu\text{C}$, distributed uniformly along its length, as shown in figure. Force between q and wire is ____ N.

(Use $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ N.m}^2 / \text{C}^2$)



Ans. (90)

Sol.



$$F = \int dF = \int_{2\text{cm}}^{12\text{cm}} \frac{kq\lambda dx}{x^2} = kq\lambda \left(\frac{1}{2 \times 10^{-2}} - \frac{1}{12 \times 10^{-2}} \right)$$

$$F = (9 \times 10^9)(10^{-6}) \left(\frac{24 \times 10^{-6}}{10^{-1}} \right) \left(\frac{5}{12} \right) \times 10^2 \\ = 9 \times 24 \times \frac{5}{12} = 90 \text{ N}$$

48. In a meter bridge experiment to determine the value of unknown resistance, first the resistances 2Ω and 3Ω are connected in the left and right gaps of the bridge and the null point is obtained at a distance l cm from the left. Now when an unknown resistance $x \Omega$ is connected in parallel to 3Ω resistance, the null point is shifted by 10 cm to the right of wire. The value of unknown resistance x is ____ Ω .

Ans. (6)

Sol. In case I

$$\frac{2}{3} = \frac{l}{(100-l)} \dots\dots(1)$$

$$l = 40 \text{ cm}$$

In case II

$$\frac{2}{R} = \frac{l+10}{100-(l+10)}$$

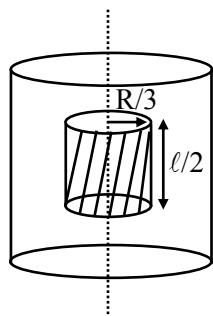
Put $l = 40 \text{ cm}$ & solve

$$R = 2\Omega$$

$$\therefore \frac{3x}{3+x} = 2$$

$$x = 6\Omega$$

49. A uniform solid cylinder of length L and radius R has moment of inertia about its axis equal to I_1 . A small co-centric cylinder of length $L/2$ and radius $R/3$ carved from this cylinder has moment of inertia about its axis equals to I_2 . The ratio I_1/I_2 is _____.
Ans. (162)

Sol.


Original mass (M)

The removed mass (m)

$$m = \rho \times \pi \left(\frac{R}{3}\right)^2 \times \frac{L}{2}$$

$$= \frac{\rho \cdot \pi R^2 L}{18} = \frac{M}{18}$$

$$I' = \frac{1}{2} \cdot \frac{M}{18} \cdot \frac{R^2}{9} = \frac{1}{324} MR^2$$

$$\frac{I}{I'} = \frac{\frac{1}{2} MR^2}{\frac{1}{324} MR^2} = 162$$



50. A soap bubble of surface tension 0.04 N/m is blown to a diameter of 7 cm. If $(15000 - x) \mu\text{J}$ of work is done in blowing it further to make its diameter 14 cm, then the value of x is _____.
 $(\pi = 22/7)$

Ans. (11304)
Sol. $W = \Delta u$

$$= S \times (8\pi r_2^2 - 8\pi r_1^2)$$

$$= 0.04 \times 2 \times \frac{22}{7} (147) \times 10^{-4}$$

$$W = 3696 \times 10^{-6} \text{ J}$$

$$3696 = 15000 - x$$

$$x = 11304 \mu\text{J}$$